

Гранична вредност низа

1. $\lim_{n \rightarrow +\infty} \frac{3n^5 + 2n^4 + 3n - 2}{7n^5 + 3n^3 + n}$.
2. $\lim_{n \rightarrow +\infty} \frac{5n^5 + 3n^3 + n}{2 + 6n^3 - 10n^5}$.
3. $\lim_{n \rightarrow +\infty} \frac{100n^3 + 2n^2}{n^4 - 100n^3 + 1}$.
4. $\lim_{n \rightarrow +\infty} \frac{(4n^2 + 1)(2n^2 - 1)}{(n^2 + 1)(n^2 + 2)(n^2 + 3)}$.
5. $\lim_{n \rightarrow +\infty} \frac{n^3 - 100n^2 + 1}{100n^2 + 20n}$.
6. $\lim_{n \rightarrow +\infty} \frac{(n^2 + 2n - 3)^3}{4n^4 + 3n^3 + 2n + 1}$.
7. $\lim_{n \rightarrow +\infty} \frac{(n+1)^3 - (n-1)^3}{(n+1)^2 + (n-1)^2}$.
8. $\lim_{n \rightarrow +\infty} \frac{(2n+1)^4 - (n-1)^4}{(2n+1)^4 + (n-1)^4}$.
9. $\lim_{n \rightarrow +\infty} \frac{(2n+1)^3 - (2n-1)^3}{(2n+1)^2 + (2n-1)^2}$.
10. $\lim_{n \rightarrow +\infty} \frac{(n^2 + 3n + 4)^3 - (n^2 + 3n - 4)^3}{(n^2 + 5n + 6)^3 - (n^2 + 5n - 6)^3}$.
11. $\lim_{n \rightarrow +\infty} \frac{(n+1)^4 - (n-1)^4}{(n^2 + 1)^2 - (n^2 - 1)^2}$.
12. $\lim_{n \rightarrow +\infty} \frac{(2n-1)^5 + (2n+1)^5}{(n+1)^5 + (n-1)^5}$.
13. $\lim_{n \rightarrow +\infty} \frac{(n^2 + 1)^3 + (n^2 + 2)^3 + \dots + (n^2 + 20)^3}{(n^3 + 1)^2 + (n^3 + 2)^2 + \dots + (n^3 + 10)^2}$.
14. $\lim_{n \rightarrow +\infty} \frac{\sqrt{n^2 + 1}}{n + \sqrt{4n^2 + 5}}$.
15. $\lim_{n \rightarrow +\infty} \frac{\sqrt[3]{n^2} + 2n}{\sqrt{n^3} + 2}$.
16. $\lim_{n \rightarrow +\infty} \frac{(n+2)! + (n+1)!}{(n+3)!}$.
17. $\lim_{n \rightarrow +\infty} \frac{(2n)!! + (2n+2)!!}{(n^2 + 1)(2n-2)!!}$.
18. $\lim_{n \rightarrow +\infty} \frac{(2n+1)!! - (2n-1)!!}{(3-n)(2n-1)!!}$.
19. $\lim_{n \rightarrow +\infty} \frac{1 + 2 + \dots + n}{(n+1)^2}$.
20. $\lim_{n \rightarrow +\infty} \frac{1^2 + 2^2 + \dots + n^2}{n^3}$.
21. $\lim_{n \rightarrow +\infty} \left(\frac{1 + 3 + \dots + (2n-1)}{n+1} - \frac{2n+1}{2} \right)$.
22. $\lim_{n \rightarrow +\infty} \frac{1 + 3 + \dots + (2n-1)}{2 + 4 + \dots + (2n)}$.
23. $\lim_{n \rightarrow +\infty} \frac{1^2 + 3^2 + \dots + (2n-1)^2}{2^2 + 4^2 + \dots + (2n)^2}$.
24. $\lim_{n \rightarrow +\infty} \frac{1 \cdot 2 + 2 \cdot 3 + \dots + n(n+1)}{n^3}$.
25. $\lim_{n \rightarrow +\infty} \frac{1 \cdot 2 \cdot 3 + 2 \cdot 3 \cdot 4 + \dots + n(n+1)(n+2)}{1^3 + 2^3 + \dots + n^3}$.
26. $\lim_{n \rightarrow +\infty} \frac{1 \cdot 3 \cdot 5 + 2 \cdot 4 \cdot 6 + \dots + n(n+2)(n+4)}{1 \cdot 3 \cdot 3 + 2 \cdot 5 \cdot 4 + \dots + n(2n+1)(n+2)}$.
27. $\lim_{n \rightarrow +\infty} \left(\frac{1}{1 \cdot 2} + \frac{1}{2 \cdot 3} + \dots + \frac{1}{n(n+1)} \right)$.
28. $\lim_{n \rightarrow +\infty} \left(\frac{1}{1 \cdot 5} + \frac{1}{5 \cdot 9} + \dots + \frac{1}{(4n-3)(4n+1)} \right)$.
29. $\lim_{n \rightarrow +\infty} \left(\frac{1}{1 \cdot 2 \cdot 3} + \dots + \frac{1}{n(n+1)(n+2)} \right)$.
30. $\lim_{n \rightarrow +\infty} \left(1 - \frac{1}{2^2} \right) \left(1 - \frac{1}{3^2} \right) \dots \left(1 - \frac{1}{n^2} \right)$.
31. $\lim_{n \rightarrow +\infty} \left(1 - \frac{1}{3} \right) \left(1 - \frac{1}{6} \right) \dots \left(1 - \frac{2}{n(n+1)} \right)$.
32. $\lim_{n \rightarrow +\infty} \frac{1}{\sqrt{n}} \left(\frac{1}{\sqrt{1} + \sqrt{3}} + \frac{1}{\sqrt{3} + \sqrt{5}} + \dots + \frac{1}{\sqrt{2n-1} + \sqrt{2n+1}} \right)$.
33. $\lim_{n \rightarrow +\infty} \left(\frac{1}{\sqrt{n^2+1}} + \frac{1}{\sqrt{n^2+2}} + \dots + \frac{1}{\sqrt{n^2+n}} \right)$.
34. $\lim_{n \rightarrow +\infty} \left(\frac{1}{\sqrt{n^2}} + \frac{1}{\sqrt{n^2+1}} + \frac{1}{\sqrt{n^2+2}} + \dots + \frac{1}{\sqrt{(n+1)^2}} \right)$.
35. $\lim_{n \rightarrow +\infty} \left(\frac{1}{\sqrt{n^4+n^2+1}} + \frac{1}{\sqrt{n^4+n^2+2}} + \dots + \frac{1}{\sqrt{n^4+11n^2}} \right)$.
36. $\lim_{n \rightarrow +\infty} (\sqrt{4n^2+3} - 2n)$.
37. $\lim_{n \rightarrow +\infty} (\sqrt{n^2-5n+6} - n)$.
38. $\lim_{n \rightarrow +\infty} (3n - \sqrt{9n^2+2n})$.
39. $\lim_{n \rightarrow +\infty} (n+2) \cdot (\sqrt{n^2+3n+2} - \sqrt{n^2+3n})$.
40. $\lim_{n \rightarrow +\infty} \frac{1}{\sqrt{n^2-5n+3} - \sqrt{n^2+3n-5}}$.
41. $\lim_{n \rightarrow +\infty} \frac{3n^2-2}{(n^4+1) \cdot (\sqrt{4n^4+3} - 2n^2)}$.
42. $\lim_{n \rightarrow +\infty} \frac{\sqrt{25n^2+4} - 5n}{4n - \sqrt{16n^2+5n}}$.
43. $\lim_{n \rightarrow +\infty} \frac{\sqrt{2n^2+2n+1} - \sqrt{2n^2-2n}}{\sqrt{4n^2+4n+1} - \sqrt{4n^2-3n}}$.
44. $\lim_{n \rightarrow +\infty} (\sqrt[3]{n+2} - \sqrt[3]{n-2})$.

$$45. \sum_{n=1}^{\infty} \frac{4^n}{n^2 + 2n}.$$

$$46. \sum_{n=1}^{\infty} \frac{n^5}{3^n + 5^n}.$$

$$47. \sum_{n=1}^{\infty} \frac{5^n + 1}{n!}.$$

$$48. \sum_{n=1}^{\infty} \frac{(2n)!}{4^n n^2}.$$

$$49. \sum_{n=1}^{\infty} \frac{n!(2n+1)!}{(3n)!}.$$

$$50. \sum_{n=1}^{\infty} \frac{(n!)^3}{(3n)!}.$$

$$51. \sum_{n=1}^{\infty} \frac{n!}{n^n}.$$

$$52. \sum_{n=1}^{\infty} \frac{(4n)!n^n}{(3n)!}.$$

$$53. \sum_{n=1}^{\infty} \frac{(\sqrt{n+1} - \sqrt{n-1})^p}{\sqrt[3]{n}}.$$

$$54. \sum_{n=1}^{\infty} \frac{(\sqrt{4n^2+1} - 2n)^p}{4n^2+1}.$$

$$55. \lim_{n \rightarrow \infty} \left(1 + \frac{1}{n}\right)^{n+3}.$$

$$56. \lim_{n \rightarrow \infty} \left(1 - \frac{2}{n+2}\right)^{3n-2}.$$

$$57. \lim_{n \rightarrow \infty} \left(1 + \frac{1-n}{2+n^2}\right)^{\frac{n}{2}}.$$

$$58. \lim_{n \rightarrow \infty} \left(\frac{2n-3}{3n+2}\right)^{n+3}.$$

$$59. \lim_{n \rightarrow \infty} \left(\frac{5n-2}{n+10}\right)^{5n}.$$

$$60. \lim_{n \rightarrow \infty} \left(\frac{n^2-n+11}{n^2-2n-1}\right)^{3n-2}.$$

$$61. \lim_{n \rightarrow \infty} \left(\frac{2n^2-n-1}{2n^2-n+1}\right)^{3-2n^2}.$$

$$62. \lim_{n \rightarrow \infty} \left(\frac{6n^2-4n+7}{6n^2-4n+5}\right)^{2n-22}.$$

$$63. \lim_{n \rightarrow \infty} \left(\frac{3n^2+3n+1}{3n^2+5n+2}\right)^{\sqrt{n}+2}.$$

$$64. \lim_{n \rightarrow \infty} n \cdot \ln\left(\frac{2n+3}{2n}\right).$$

$$65. \lim_{n \rightarrow \infty} n^2 \left(\ln n \left(n + \frac{1}{n}\right) - \ln n^2\right).$$

$$66. \lim_{n \rightarrow \infty} \left(\frac{n^2+2n+3}{(n+1)^2}\right)^{1+2+\dots+n}.$$

$$67. \lim_{n \rightarrow \infty} \left(\frac{n^2+4n+6}{(n+2)^2}\right)^{\frac{1^2+2^2+\dots+n^2}{n}}.$$

$$68. \lim_{n \rightarrow \infty} \frac{5n+3^n}{3n+5^n}.$$

$$69. \lim_{n \rightarrow \infty} \frac{2^n+3^n}{2^{n+1}+3^{n+1}}.$$

$$70. \lim_{n \rightarrow \infty} \frac{2^n+3n^3}{n^5+3 \cdot 2^{n+1}}.$$

$$71. \lim_{n \rightarrow \infty} \frac{n^2+n!}{3^n-(n+1)!}.$$

$$72. \lim_{n \rightarrow \infty} \frac{4^n+n^2 2^n-1}{n^4+(n!)^2}.$$

$$73. \lim_{n \rightarrow \infty} \frac{n^2+n!}{(2n)!}.$$

$$74. \lim_{n \rightarrow \infty} n(\ln(2^n+3) - \ln(2^n+1)).$$

$$75. \lim_{n \rightarrow \infty} \left(1 + \frac{1}{2} + \frac{1}{2^2} + \dots + \frac{1}{2^{n-1}}\right).$$

$$76. \lim_{n \rightarrow \infty} \left(5 - \frac{1}{2} - \frac{1}{2^2} - \dots - \frac{1}{2^{n-1}}\right).$$

$$77. \lim_{n \rightarrow \infty} \frac{2+2^2+\dots+2^n}{3+3^2+\dots+3^n}.$$

$$78. \lim_{n \rightarrow \infty} \sqrt{2} \cdot \sqrt[4]{2} \cdot \dots \cdot \sqrt[2^n]{2}.$$

$$79. \lim_{n \rightarrow \infty} \sqrt[4]{7} \cdot \sqrt[16]{7} \cdot \dots \cdot \sqrt[4^n]{7}.$$

80. Одредити вредност параметра $p \neq 0$ тако да $\lim_{n \rightarrow \infty} (a_n)$ буде коначан:

$$a) a_n = \frac{n^2-n+2}{pn+1} - \frac{pn^2-1}{2n-3};$$

$$б) a_n = \frac{2pn^3-2n}{4n^2-3n} - \frac{3n-2n^2}{2-pn}.$$

81. Одредити вредност параметра p тако да је $\lim_{n \rightarrow \infty} (a_n) = 0$:

$$a) a_n = \frac{p^2 n^2 + 3}{n^2 + 5n + 6} - \frac{2 + 4n}{3 + n};$$

$$б) a_n = \frac{\sqrt{n+p}}{3p+p\sqrt{n}} - \frac{3+p\sqrt{n}}{\sqrt{n+2}}, p \neq 0.$$

82. Одредити вредност параметра $p \neq 0$ тако да је $\lim_{n \rightarrow \infty} (a_n) = 1$:

$$a) a_n = \left(\frac{n^2+pn+p+1}{n^2-7n+1}\right)^{n-3};$$

$$б) a_n = \left(\frac{pn^2+3n-p}{pn^2-pn+2}\right)^n;$$

$$в) a_n = \left(\frac{n^3+2pn^2+3n}{n^3+5n^2-p}\right)^{\frac{n+1}{2}}.$$

83. Одредити вредност параметра p тако да је $\lim_{n \rightarrow \infty} (a_n) = 0$:

$$a) a_n = \left(\frac{n^2+pn+2}{n^2+3n+1}\right)^{(p-1)n^2+n};$$

$$б) a_n = \left(\frac{3n^2-pn+6}{pn^2+2n-3}\right)^n;$$

$$в) a_n = n \cdot (\ln(pn^2+3n-p) - \ln(pn^2-pn+2)).$$

$$84. \lim_{n \rightarrow \infty} \left(1 - \frac{9}{2^2}\right) \left(1 - \frac{9}{5^2}\right) \cdots \left(1 - \frac{9}{(3n-1)^2}\right).$$

$$85. \lim_{n \rightarrow \infty} \frac{2^3 - 1}{2^3 + 1} \cdot \frac{3^3 - 1}{3^3 + 1} \cdots \frac{n^3 - 1}{n^3 + 1}.$$

$$86. \lim_{n \rightarrow +\infty} \left(\frac{1}{\sqrt{n^2 + 2}} + \frac{1}{\sqrt{n^2 + 4}} + \cdots + \frac{1}{\sqrt{n^2 + 6n}} \right).$$

$$87. \lim_{n \rightarrow +\infty} \left(\frac{1}{\sqrt{n^2}} + \frac{1}{\sqrt{n^2 + 1}} + \cdots + \frac{1}{\sqrt{(n+1)^2}} \right).$$

$$88. \lim_{n \rightarrow +\infty} \left(\frac{1}{\sqrt{n^4 + n^2 + 1}} + \frac{1}{\sqrt{n^4 + n^2 + 2}} + \cdots + \frac{1}{\sqrt{n^4 + 11n^2}} \right).$$

$$89. \lim_{n \rightarrow +\infty} \left(\frac{1}{\sqrt[3]{n^3 + 1}} + \frac{1}{\sqrt[3]{n^3 + 2}} + \cdots + \frac{1}{\sqrt[3]{n^3 + n}} \right).$$

$$90. \lim_{n \rightarrow +\infty} \left(\frac{1}{\sqrt[3]{n^3 + n^2 + 1}} + \frac{1}{\sqrt[3]{n^3 + n^2 + 2}} + \cdots + \frac{1}{\sqrt[3]{n^3 + n^2 + 5n}} \right).$$

$$91. \lim_{n \rightarrow +\infty} \left(\frac{1}{\sqrt[3]{8n^3 + 1}} + \frac{1}{\sqrt[3]{8n^3 + 2}} + \cdots + \frac{1}{\sqrt[3]{8n^3 + 2n}} \right).$$

92. Одредити тачке нагомилавања низа a_n :

а) $a_n = 1 + 2(-1)^{n-1} + 3(-1)^{n(n+1)}$;
 $\frac{2^n + 3^n}{2^n + 3^n}$;

б) $a_n = \frac{(-2)^{n+1} + (-3)^{n+1}}{3n^2 + 2n + 1}$;

в) $a_n = \frac{(-1)^n n^2 + 3n + 2}{(-1)^n n^2 + 3n + 2}$;

г) $a_n = (-1)^n \cdot \left(\frac{3n+2}{3n-2}\right)^{2n}$;

д) $a_n = (-1)^n \cdot \left(1 - \frac{5}{n}\right)^{2n} + \frac{n-3}{2n+5}$;

ђ) $a_n = \left(\frac{n+1}{n+3}\right)^{3n} \cdot \cos n\pi$;

е) $a_n = 1 + \frac{n^{-3} + 1}{n^{-3} + 2} \cdot \cos \frac{n\pi}{2}$;

ж) $a_n = \left(\frac{2n^{-1} + 3}{5n^{-1} + 3}\right)^{\frac{n}{3}} + \sqrt[3]{\pi} \cdot \cos \frac{n\pi}{3}$;

з) $a_n = (-1)^n \cdot \left(1 + \frac{3}{n}\right)^{2n} + \frac{n}{\sqrt{n^2 + 1}} \cdot \cos \frac{n\pi}{3}$;

и) $a_n = \frac{2-n}{5n-1} \cdot \sin \frac{n\pi}{4}$;

ж) $a_n = (-1)^n \cdot (n - \sqrt{n^2 + n})^3 + \sin \frac{n\pi}{3}$;

93. Одредити $\overline{\lim}_{n \rightarrow \infty} (a_n) = \limsup_{n \rightarrow \infty} (a_n)$ и $\underline{\lim}_{n \rightarrow \infty} (a_n) = \liminf_{n \rightarrow \infty} (a_n)$:

а) $a_n = \left(\sqrt[3]{\frac{n+1}{n}}\right)^n \cos \frac{2n\pi}{3} + (-1)^n \cdot \frac{2n^2 - 3}{3n^2 + 2}$;

б) $a_n = \frac{2n^{-2} - 5}{6 - n^{-1}} \cdot \sin \frac{n\pi}{3}$;

в) $a_n = (-1)^n \cdot \left(1 + \frac{2}{n}\right)^{5n} + \sin \frac{n\pi}{4}$;

94. Доказати да је низ (a_n) , задат рекурентном формулом, конвергентан и наћи $\lim_{n \rightarrow \infty} (a_n)$:

а) $a_1 = 3, a_{n+1} = \frac{a_n + 1}{2}, n \in \mathbf{N}$;

б) $a_1 = 1, a_{n+1} = \sqrt{2 + a_n}, n \in \mathbf{N}$;

в) $a_1 = 1, a_{n+1} = \frac{a_n}{a_n + 2}, n \in \mathbf{N}$;

г) $a_1 = \frac{1}{2}, a_{n+1} = \frac{2a_n}{1 + a_n^2}, n \in \mathbf{N}$;

д) $a_1 = 1, a_{n+1} = \frac{2(2a_n + 1)}{a_n + 3}, n \in \mathbf{N}$;

ђ) $a_1 = 2, a_{n+1} = \frac{4a_n}{a_n + 3}, n \in \mathbf{N}$;

е) $a_1 = 2, a_{n+1} = \frac{a_n^2}{2a_n - 1}, n \in \mathbf{N}$;

ж) $a_1 = 3, a_{n+1} = \frac{1}{2} \left(a_n + \frac{3}{a_n}\right), n \in \mathbf{N}$;

з) $a_1 = \frac{7}{2}, a_{n+1} = \frac{a_n^2 - 6}{2a_n - 5}, n \in \mathbf{N}$;

и) $a_1 = 2, a_{n+1} = \frac{3a_n + 4}{a_n + 6}, n \in \mathbf{N}$;

ј) $a_1 = \frac{1}{2}, a_{n+1} = a_n^3 - 2a_n^2 + a_n, n \in \mathbf{N}$;

к) $a_1 = 1, a_{n+1} = \sqrt[3]{6 + a_n}, n \in \mathbf{N}$;

л) $a_1 = 1, a_{n+1} = \sqrt[3]{2a_n + 4}, n \in \mathbf{N}$;

љ) $a_1 = -4, a_{n+1} = \sqrt[3]{3 + a_n - 3a_n^2}, n \in \mathbf{N}$;

м) $a_1 = \sqrt{3}, a_{n+1} = \sqrt{3 + a_n}, n \in \mathbf{N}$;

н) $a_1 = 4, a_{n+1} = \sqrt{6 + a_n}, n \in \mathbf{N}$;

95. $\lim_{n \rightarrow \infty} \left(1 + \frac{1-n}{2+n^2}\right)^{\frac{n}{2}}$.

96. $\lim_{n \rightarrow \infty} \left(\frac{2n-3}{3n+2}\right)^{n+3}$.

97. $\lim_{n \rightarrow \infty} \left(\frac{5n-2}{n+10}\right)^{5n}$.

98. $\lim_{n \rightarrow \infty} \left(\frac{3n^2 - n + 11}{3n^2 - 2n - 1}\right)^{3n-2}$.

99. $\lim_{n \rightarrow \infty} \left(\frac{(n+1)(n-4) - 3}{(n-2)(n+1)}\right)^{4n}$.

100. $\lim_{n \rightarrow \infty} \frac{\left(\frac{2n^2 - 2n}{3n-4}\right)^{2n^2 - 2n}}{2n^2 + 7n - 6}$.

101. $\lim_{n \rightarrow \infty} n^2 \left(\ln n^2 \left(n + \frac{1}{n}\right) - 3 \ln n\right)$.

102. $\lim_{n \rightarrow \infty} \frac{\left(\frac{n^2 + 2n + 3}{(n+1)^2}\right)^{1+2+\dots+n}}{3}$.

103. $\lim_{n \rightarrow \infty} \sqrt{2} \cdot \sqrt[4]{2} \cdots \sqrt[2^n]{2}$.

104. $\lim_{n \rightarrow \infty} \sqrt{3} \cdot \sqrt[4]{3} \cdots \sqrt[2^n]{3}$.

105. $\lim_{n \rightarrow \infty} \sqrt[3]{5} \cdot \sqrt[9]{5} \cdots \sqrt[3^n]{5}$.

106. $\lim_{n \rightarrow \infty} \sqrt[4]{7} \cdot \sqrt[16]{7} \cdots \sqrt[4^n]{7}$.

107. $\lim_{n \rightarrow \infty} \underbrace{\sqrt{8\sqrt{8\sqrt{8\cdots\sqrt{8}}}}}_{n \text{ корена}}$.

108. $\lim_{n \rightarrow \infty} \underbrace{\sqrt[3]{9\sqrt[3]{9\sqrt[3]{9\cdots\sqrt[3]{9}}}}}_{n \text{ корена}}$.

109. $\lim_{n \rightarrow \infty} \left(5 - \frac{1}{2} - \frac{1}{2^2} - \cdots - \frac{1}{2^{n-1}}\right)$.

$$110. \lim_{n \rightarrow \infty} \left(1 - \frac{3}{4} + \frac{9}{16} - \frac{27}{64} + \dots + (-1)^n \left(\frac{3}{4} \right)^n \right).$$

Додатак, 13.5.2013:

$$1. \lim_{n \rightarrow \infty} \frac{\sqrt{25n^2 + 4n} - 5n}{4n - \sqrt{16n^2 + 5n}}.$$

$$2. \lim_{n \rightarrow \infty} (n + \sqrt[3]{n^2 - n^3}).$$

$$3. \lim_{n \rightarrow \infty} \frac{\sqrt[3]{n^4 + 4n^3 + 5n - 2} - \sqrt[3]{n^4 + 2n - 1}}{\sqrt[3]{n + 1}}.$$

$$4. \lim_{n \rightarrow \infty} \frac{\sqrt[4]{n^4 + 4} - n}{2n - \sqrt[4]{16n^4 + 1}}.$$

$$5. \lim_{n \rightarrow \infty} \frac{\sqrt[4]{n^4 + 2n} - n}{\sqrt[3]{8n^3 + 1} - 2n}.$$

$$6. \lim_{n \rightarrow \infty} \frac{\sqrt[3]{n^3 + n^2 - 1} - n}{\sqrt[4]{n^4 + 3n^3 + 2} - n}.$$

$$7. \lim_{n \rightarrow \infty} \left(5 - \frac{1}{2} - \frac{1}{2^2} - \dots - \frac{1}{2^{n-1}} \right).$$

$$8. \lim_{n \rightarrow \infty} \left(1 - \frac{3}{4} + \frac{9}{16} - \frac{27}{64} + \dots + (-1)^n \left(\frac{3}{4} \right)^n \right).$$

9. Одредити вредност параметра $p \neq 0$, тако да $\lim_{n \rightarrow \infty} (a_n)$ буде коначан:

$$(a) a_n = \frac{n^2 - n + 2}{pn + 1} - \frac{pn^2 - 1}{2n - 3};$$

$$(б) a_n = \left(n^2 - \frac{(n+p)^3}{n-2} \right).$$

10. Одредити вредност параметра p тако да је $\lim_{n \rightarrow \infty} (a_n) = 0$:

$$(a) a_n = \frac{pn + 3}{n - 2} + \frac{n - p}{3 - 2n};$$

$$(б) a_n = \frac{p^2\sqrt{n} + 2}{\sqrt{n} + 1} + \frac{2p - \sqrt{4n}}{\sqrt{n} - 1}. \quad (в) a_n = \frac{p\sqrt{n} + 3}{\sqrt{n} + 4} + \frac{5p + p^2\sqrt{n}}{\sqrt{n} - 4}$$

11. Одредити вредност параметра p тако да је $\lim_{n \rightarrow \infty} (a_n) = 1$:

$$(a) a_n = \left(\frac{pn^2 + 3n - p}{pn^2 - pn + 2} \right)^n, \quad p \neq 0;$$

$$(б) a_n = \left(\sqrt{\frac{n^3 + 2pn^2 + 3n}{n^3 + 5n^2 - p}} \right)^{n+1}.$$

12. Одредити вредност параметра p тако да је $\lim_{n \rightarrow \infty} (a_n) = 0$:

$$(a) a_n = \left(\frac{n^2 + pn + 2}{n^2 + 3n + 1} \right)^{(p-1)n^2 + n};$$

$$(б) a_n = \left(\frac{3n^2 - pn + 6}{3n^2 + 2n - 3} \right)^{n^2 - 5n}.$$